# LOCATA CHALLENGE - OVERVIEW OF EVALUATION MEASURES

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### **ABSTRACT**

This document provides an overview of the evaluation measures used for the LOCATA challenge. The contents of this document are an excerpt from a manuscript submitted to IWAENC 2018.

### 1. EVALUATION MEASURES

This section provides an overview of performance measures used for evaluation of the LOCATA Challenge. As all estimates must be associated with an Identifier (ID), the estimates resulting from localization and tracking algorithms alike are referred to as "tracks" in the following.

### 1.1. Nomenclature

Consider a single recording of duration  $\Delta_{\rm rec}$ , including a maximum number of  $N_{\rm max}$  sources. Each source  $n \in \{1,\ldots,N_{\rm max}\}$  corresponds to A(n) periods of activity of duration  $\Delta(a,n) = t_{\rm end}(a,n) - t_{\rm srt}(a,n)$  for  $a \in \{1,\ldots,A(n)\}$ , where  $t_{\rm srt}(a,n)$  and  $t_{\rm end}(a,n)$ , respectively, mark the start and end time of the activity period. The corresponding time indices are  $\{\ell_{\rm srt}(a,n),\ell_{\rm end}(a,n)\} \geq 0$ . Each activity period corresponds to an utterance of speech, which is assumed to include voiced and unvoiced segments.

For each time step t, a localization and t or tracking algorithm estimates the source positional information in a given coordinate system, resulting in K(t) track state estimates,  $\mathbf{x}_i(t), i=1,\ldots,K(t)$  for each  $t\in\{1,\ldots,\Delta_{\rm rec}\}$ . Each state estimate is associated with a unique track ID. We note that the evaluation measures detailed in the following are independent of any specific coordinate system, i.e.,  $\mathbf{x}_i(t)$  is used in a general form and could describe, for example, the source azimuth, elevation, or 3D Cartesian position.

Gating combined with association algorithms [1] leads to an assignment of each track to the nearest ground-truth source position. In practice, tracks are subject to estimation errors. Furthermore, the assignment is subject to ambiguities [2, 3, 1] (see Fig. 1):

**Valid track:** Track associated to one source.  $\Delta_{\text{valid}}(a,n)$  and  $L_{\text{valid}}(a,n)$  respectively denote the duration and the number of time steps in which source n is associated with a valid track during activity period a.

**Redundant track:** Associated with a source that is already associated with one or more tracks.

False track: Not associated with any source.

Missing track: No track associated with a particular sources

**Broken track:** A valid track whose association is temporarily "interrupted", i.e., the track is not associated with any source for one or more time steps.

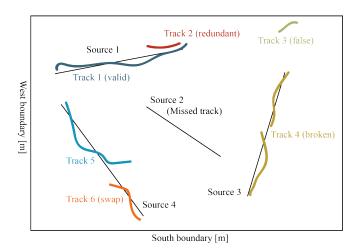


Fig. 1. Tracking ambiguities. Colors indicate unique track IDs.

**Track swap:** Source n is associated with track k at t-1, and with track  $j \neq k$  at t.

To provide a balanced evaluation, the LOCATA Challenge relies on multiple, complementary performance measures in order to reflect track quality, in addition to the accuracy, in terms of ambiguity, completeness, continuity, and timeliness [2].

## 1.2. Fixed Track-to-Source Association

A one-to-one assignment between sources and tracks is established using the association algorithm in [4]. Based on the track-to-source association, the following evaluation measures are used.

### 1.2.1. Absolute Track Accuracy

The angular errors [5] of the tracked source azimuth and elevation respectively, as well as the absolute error in the estimated range are evaluated for each recording, source, activity period, and time step. The Euclidean distance between the ground-truth and tracked Cartesian positions is also evaluated.

### 1.2.2. Track Ambiguity

The track IDs provided by the participants are used to evaluate the number of valid,  $K_{\rm valid}(t)$ , false,  $K_{\rm false}(t)$ , missing,  $K_{\rm miss}(t)$ , broken,  $K_{\rm broken}(t)$ , and swapped,  $K_{\rm swap}(t)$ , tracks for each time step t.

To further quantify ambiguities, the following measures are incorporated in the challenge evaluation:

**Probability of detection**  $(p_d)$  [1]: A measure of track completeness, comparing the number of time stamps during which an active source was detected to the total number of time stamps in activity period, a:

$$p_d(a,n) = \frac{L_{\text{valid}}(a,n)}{\ell_{\text{end}}(a,n) - \ell_{\text{srt}}(a,n) + 1}.$$

- False Alarm Rate (FAR) [2]: A measure of track ambiguity, comparing the number of false tracks to the number of time steps per recording.
- **Track Latency** (TL) [2]: A measure of track timeliness, indicating the delay between the onset and detection of source n in activity period a.
- **Track Fragmentation Rate (TFR)** [6]: A measure of track continuity, indicating the number changes in the track IDs assigned to an active source.

We note that the one-to-one assignment obtained using [4] avoids redundant tracks.

### 1.3. Permutations of Track-to-Source Associations

Measures using fixed source-to-track association potentially penalize the tracker for ambiguities in the assignment process during evaluation between the source ground truth and the tracks. The Optimal Subpattern Assignment (OSPA) distance relaxes penalties for association ambiguities by evaluating all permutations of track-to-source associations at each time step. Moreover, the OSPA distance [7, 8] provides a combined measure of the accuracy, continuity, and FAR:

$$OSPA(\mathbf{X}(t), \mathbf{Y}(t)) \triangleq$$

$$\left[\frac{1}{K(t)} \min_{\pi \in \Pi_{K(t)}} \sum_{n=1}^{N(t)} d_c(\mathbf{y}_n(t), \mathbf{x}_{\pi(n)}(t))^p + (K(t) - N(t))c^p\right]^{\frac{1}{p}},$$

where  $\mathbf{X}(t) \triangleq \{\mathbf{x}_1(t), \dots, \mathbf{x}_{K(t)}(t)\}$  denotes the set of K(t) track estimates;  $\mathbf{Y}(t) \triangleq \{\mathbf{y}_1(t), \dots, \mathbf{y}_{N(t)}(t)\}$  denotes the set of N(t) sources active at  $t; 1 \leq p < \infty$  marks the order parameter; c is the cutoff parameter;  $\mathbf{\Pi}_{K(t)}$  denotes the set of permutations of length N(t) with elements  $\{1, \dots, K(t)\}; d_c(\mathbf{y}_n(t), \mathbf{x}_{\pi(i)}(t)) \triangleq \min(c, d(\mathbf{y}_n(t), \mathbf{x}_{\pi(i)}(t)));$  and  $d(\cdot)$  is the measure of accuracy (see Sec. 1.2.1). The impact of the choice of p and c is discussed in [9].

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